

Floating-point control in the Intel® C/C++
compiler and libraries
or
Why doesn't my application always give the
same answer?

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Agenda

- Overview
- Floating Point (FP) Model
 - Comparisons with gcc
- Performance impact
- Runtime math libraries
- Intel® Xeon Phi™ Coprocessors – what's different

Overview

- The finite precision of floating-point operations leads to an inherent uncertainty in the results of a floating-point computation
 - Results may vary within this uncertainty
- Nevertheless, may need reproducibility beyond this uncertainty
 - For reasons of Quality Assurance, e.g. when porting, optimizing, etc
- The right compiler options can deliver consistent, closely reproducible results whilst preserving good performance
 - Across IA-32, Intel® 64 and other IEEE-compliant platforms
 - Across optimization levels
 - -fp-model is the recommended high level control for the Intel Compiler

Floating Point (FP) Programming Objectives

- **Accuracy**

- Produce results that are “close” to the correct value
 - Measured in relative error, possibly in ulp

- **Reproducibility**

- Produce consistent results
 - From one run to the next
 - From one set of build options to another
 - From one compiler to another
 - From one platform to another

- **Performance**

- Produce the most efficient code possible

These options usually conflict!

Judicious use of compiler options lets you control the tradeoffs.
Different compilers have different defaults.

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Floating Point Semantics

- The `-fp-model (/fp:)` switch lets you choose the floating point semantics at a coarse granularity. It lets you specify the compiler rules for:
 - **Value safety** (main focus)
 - FP expression evaluation
 - FPU environment access
 - Precise FP exceptions
 - FP contractions (fused multiply-add)
- Also pragmas in C99 standard
 - `#pragma STDC FENV_ACCESS` etc
- Old switches such as `-mp` now deprecated
 - Less consistent and incomplete; don't use

The `-fp-model` switch for `icc`

● **`-fp-model`**

- `fast [=1]` allows value-unsafe optimizations (default)
- `fast=2` allows additional approximations
- `precise` value-safe optimizations only
- `source | double | extended` imply “precise” unless overridden
see “FP Expression Evaluation” for more detail
- `except` enable floating point exception semantics
- `strict` precise + except + disable fma +
don’t assume default floating-point

environment

- Replaces old switches `-mp`, `-fp-port`, etc (don’t use!)

• **`-fp-model precise` `-fp-model source`**

- recommended for ANSI/ IEEE standards compliance, C+
+ & Fortran

– “source” is default with “precise” on Intel 64 Linux

GCC option

- -f[no-]fast-math is high level option
 - It is **off by default** (different from icc)
 - It is turned on by -Ofast
- Components control similar features:
 - Value safety (-funsafe-math-optimizations)
 - includes reassociation
 - Reproducibility of exceptions
 - assumptions about floating-point environment
 - Assumptions about exceptional values
- also sets abrupt/gradual underflow (FTZ)
- For more detail, check backup or <http://gcc.gnu.org/wiki/FloatingPointMath>

Value Safety

- In SAFE mode, the compiler may not make any transformations that could affect the result, e.g. all the following are prohibited.

$$x / x \Leftrightarrow 1.0$$

x could be 0.0, ∞ , or NaN

$$x - y \Leftrightarrow -(y - x)$$

If x equals y, $x - y$ is +0.0 while $-(y - x)$ is -0.0

$$x - x \Leftrightarrow 0.0$$

x could be ∞ or NaN

$$x * 0.0 \Leftrightarrow 0.0$$

x could be -0.0, ∞ , or NaN

$$x + 0.0 \Leftrightarrow x$$

x could be -0.0

$$(x + y) + z \Leftrightarrow x + (y + z)$$

General reassociation is not value safe

$$(x == x) \Leftrightarrow \text{true}$$

x could be NaN

Value Safety

Affected Optimizations include:

- Reassociation
- Flush-to-zero
- Expression Evaluation, various mathematical simplifications
- Approximate divide and sqrt
- Math library approximations

Reassociation

- Addition & multiplication are “associative” (& distributive)
 - $a+b+c = (a+b) + c = a + (b+c)$
 - $a*b + a*c = a * (b+c)$
- These transformations are equivalent ***mathematically***
 - but ***not*** in finite precision arithmetic
- Reassociation can be disabled in its entirety
 - $\Rightarrow$ for standards conformance (C left-to-right)
 - Use **-fp-model precise**
 - May carry a significant performance penalty (other optimizations also disabled)
- Parentheses are respected only in value-safe mode!
 - -assume protect_parens compromise (Fortran only)
- See exercises for an example derived from a real app

Example (see exercises)

"tiny" is intended to keep $a[i] > 0$

but... optimizer hoists constant
expression ($c + \text{tiny}$) out of loop
tiny gets "rounded away" wrt c

```
icc -O1 reassoc.cpp; ./a.out
```

```
a = 0  b = inf
```

```
icc -fp-model precise reassoc.cpp; ./a.out
```

```
a = 1e-20  b = 1e+20
```

```
g++ reassoc.cpp; ./a.out
```

```
a = 1e-20  b = 1e+20
```

```
g++ -O3 -ffast-math reassoc.cpp; ./a.out
```

```
a = 0  b = inf
```

```
#include <iostream>
#define N 100

int main() {
    float a[N], b[N];
    float c = -1., tiny = 1.e-20F;

    for (int i=0; i<N; i++) a[i]=1.0;

    for (int i=0; i<N; i++) {
        a[i] = a[i] + c + tiny;
        b[i] = 1/a[i];
    }
    std::cout << "a = " << a[0] <<
        "  b = " << b[0] << "\n";
}
```

Denormalized numbers and Flush-to-Zero (FTZ)

- Denormals extend the (lower) range of IEEE floating-point values, at the cost of:
 - Reduced precision
 - Reduced performance (can be 100 X for ops with denormals)
- If your application creates but does not depend on denormal values, setting these to zero may improve performance (“abrupt underflow”, or “flush-to-zero”,)
 - Done in Intel® SSE or Intel® AVX hardware, so fast
 - Happens by default at -O1 or higher (for icc, not gcc)
 - -no-ftz or -fp-model precise will prevent
 - Must compile main with this switch to have an effect
 - -fp-model precise -ftz to get “precise” without denormals
 - Not available for x87, denormals always generated
 - (unless trapped and set to zero in software – very slow)
- For gcc, -ffast-math sets abrupt underflow (FTZ)
 - But -O3 -ffast-math reverts to gradual underflow

Reductions

- Parallel implementations imply reassociation (partial sums)
 - Not value safe, but can give substantial performance advantage
 - -fp-model precise
 - disables vectorization of reductions
 - except those mandated by Intel® Cilk Plus
 - does not affect OpenMP* or MPI* reductions

These remain value-unsafe
(programmer's responsibility)

```
float Sum(const float A[], int n )
{
    float sum=0;
    for (int i=0; i<n; i++)
        sum = sum + A[i];
    return sum;
}
```

```
float sum( const float A[], int n )
{
    int i, n4 = n-n%4;
    float sum=0, sum1=0, sum2=0, sum3=0;
    for (i=0; i<n4; i+=4) {
        sum  = sum  + A[i];
        sum1 = sum1 + A[i+1];
        sum2 = sum2 + A[i+2];
        sum3 = sum3 + A[i+3];
    }
    sum = sum + sum1 + sum2 + sum3;
    for (; i<n; i++) sum = sum + A[i];
    return sum;
}
```

Reproducibility of Reductions in OpenMP*

- Each thread has its own partial sum
 - Breakdown, & hence results, depend on number of threads
 - Partial sums are summed at end of loop
 - Order of partial sums is undefined (OpenMP standard)
 - First come, first served
 - Result may vary from run to run (even for same # of threads)
 - For both gcc and icc
 - Can be more accurate than serial sum
 - For icc & ifort, option to define the order of partial sums (tree algorithm)
 - Makes results reproducible from run to run
 - export KMP_DETERMINISTIC_REDUCTION=yes (in 13.0)
 - May also help accuracy
 - Possible slight performance impact, depends on context
 - Requires static scheduling, fixed number of threads
 - Default for large numbers of threads

FP Expression Evaluation

- In the following expression, what if a, b, c, and d are mixed data types (single and double for example)

$a = (b + c) + d$

Four possibilities for **intermediate** rounding, (corresponding to C99 FLT_EVAL_METHOD)

Indeterminate	(-fp-model fast)
Use precision specified in source	(-fp-model source)
Use double precision (C/C++ only)	(-fp-model double)
Use long double precision (C/C++ only)	(-fp-model extended)

- Or platform-dependent default (-fp-model precise)
 - Defaults to **-fp-model source** on Intel64
 - Recommended for most purposes
- The expression evaluation method can significantly impact performance, accuracy, and portability

The Floating Point Unit (FPU) Environment

- FP Control Word Settings
 - Rounding mode (nearest, toward $+\infty$, toward $-\infty$, toward 0)
 - Exception masks, status flags (inexact, underflow, overflow, divide by zero, denormal, invalid)
 - Flush-to-zero (FTZ), Denormals-are-zero (DAZ)
 - x87 precision control (single, double, extended) [don't mess!]
- Affected Optimizations, e.g.
 - Constant folding (evaluation at compile time)
 - FP speculation
 - Partial redundancy elimination
 - Common subexpression elimination
 - Dead code elimination
 - Conditional transform, e.g.
if (c) x = y; else x = z; $\rightarrow$ x = (c) ? y : z;

FPU Environment Access

- When access disabled (default):
 - compiler assumes default FPU environment
 - Round-to-nearest
 - All exceptions masked
 - No FTZ/DAZ
 - Compiler assumes program will NOT read status flags
- If user might change the default FPU environment, inform compiler by setting FPU environment access mode!!
 - Access may only be enabled in value-safe modes, by:
 - **-fp-model strict** or
 - `#pragma STDC FENV_ACCESS ON`
 - Compiler treats control settings as unknown
 - Compiler preserves status flags
 - Some optimizations are disabled
- If you forget this, you might get **completely** wrong results!
 - Eg from math functions, if you change default rounding mode

Example

```
double  x.,  zero = 0.;
    feenableexcept
(FE_DIVBYZERO);

    for( int i = 0; i < 20; i+
+ )
```

Problem: F-P exception from `x = zero ? (1./zero) : zero;` despite explicit protection

- The invariant `(1./zero)` gets speculatively hoisted out of loop by optimizer, but the “?” alternative does not
- Compiler thinks safe, because exceptions are masked by default
- exception occurs before the protection can kick in
 - may not occur for Intel® AVX, which have masked vector instructions

Solution: Disable optimizations that lead to the premature exception

- `icc -fp-model strict`
warns compiler that F-P defaults have been modified
- `#pragma STDC FENV_ACCESS ON` does likewise
- `icc -fp-speculation safe`
disables just speculation where this could cause an exception

Precise FP Exceptions

- When Disabled (default):
 - Code may be reordered by optimization
 - FP exceptions might not occur in the “right” places
- When enabled by
 - fp-model strict
 - fp-model except
 - #pragma float_control(except, on)
 - The compiler must account for the possibility that any FP operation might throw an exception
 - Disables optimizations such as FP speculation
 - May only be enabled in value-safe modes
 - (more complicated for x87)
 - Does not unmask exceptions
 - Must do that separately, e.g.
 - fp-trap=common for C
 - or functions calls such as feenableexcept()
 - fpe0 or ieee set halting mode() for Fortran

Floating Point Contractions

- affects the generation of FMA instructions on Intel® MIC architecture and Intel® AVX2 (`-xcore-avx2`)
 - Enabled by default or `-fma`, disable with `-no-fma`
 - Disabled by `-fp-model strict` or C/C++ `#pragma`
 - NOT disabled by `-fp-model precise`
 - `-[no-]fma` switch overrides `-fp-model` setting
 - Intel compiler does NOT support 4-operand AMD*-specific fma instruction)
- When enabled:
 - The compiler may generate FMA for combined multiply/add
 - Faster, more accurate calculations
 - Results may differ in last bit from separate multiply/add
- When disabled:
 - `-fp-model strict`, `#pragma fp_contract(off)` or `-no-fma`
 - The compiler must generate separate multiply/add with intermediate rounding

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Typical Performance Impact of -fp-model source

- Measured on SPECCPU2006fp benchmark suite:
- -O2 or -O3
- Geomean reduction due to
-fp-model precise -fp-model source
in range 12% - 15%
- Intel® Compiler XE 2011 (12.0)
- Measured on Intel Xeon® 5650 system with dual, 6-core processors at 2.67Ghz, 24GB memory, 12MB cache, SLES* 10 x64 SP2

Use -fp-model source (/fp:source) to improve floating point reproducibility whilst limiting performance impact

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Math Library Functions

- Different implementations may not have the same accuracy
 - On Intel 64:
 - libsvml for vectorized loops
 - libimf (libm) elsewhere
 - Processor-dependent code within libraries, selected at runtime
 - Inlining was important for Itanium, to get software pipelining, but less important for Intel 64 since can vectorize with libsvml
 - Used for some division and square root implementations
- No official standard (yet) dictates accuracy or how results should be rounded (except for division & sqrt)
- fp-model precise helps generate consistent math calls
 - eg within loops, between kernel & prolog/epilog
 - Remove or reduce dependency on alignment
 - May prevent vectorization unless use -fast-transcendentals
 - When may differ from non-vectorized loop

Select minimum precision

- Currently for libsvml (vector); scalar libimf normally “high”

New math library features (12.x compiler)

- Default is off (compiler chooses)
- Typically high for scalar code, medium for vector code
- “low” typically halves the number of mantissa bits
 - Potential performance improvement
- “high” ~0.55 ulp; “medium” < 4 ulp (typically 2)

`-fimf-arch-consistency=<true | false>`

- Will produce consistent results on all microarchitectures or processors within the same architecture
- Run-time performance may decrease
- Default is false (even with `-fp-model precise` !)

Math Libraries – potential issues

- Differences could potentially arise between:
 - Different compiler releases, due to algorithm improvements
 - Use `-fimf-precision`
 - another workaround, use later RTL with both compilers
 - Different platforms, due to different algorithms or different code paths at runtime
 - Libraries detect run-time processor internally
 - Independent of compiler switches
 - use `-fimf-arch-consistency=true`
 - Expected accuracy is maintained
 - 0.55 ulp for libimf
 - < 4 ulp for libsvml (default for vectorized loops)
- Adherence to an eventual standard for math functions would improve consistency but at a cost in performance.

Intel® Math Kernel Library

- Linear algebra, FFTs, sparse solvers, statistical, ...
 - Highly optimized, vectorized
 - Threaded internally using OpenMP*
 - By default, repeated runs may not give identical results
- **Conditional BitWise Reproducibility (new)**
 - Repeated runs give identical results under certain conditions:
 - Same number of threads
 - OMP_SCHEDULE=static (the default)
 - Same OS and architecture (e.g. Intel 64)
 - Same microarchitecture, or specify a minimum microarchitecture
 - Consistent data alignment
 - Call `mkl_cbwr_set(MKL_CBWR_COMPATIBLE)`
 - Or set environment variable `MKL_CBWR_BRANCH="COMPATIBLE"`
 - In Intel® Composer XE 2013

Intel® Threading Building Blocks

- A C++ template library for parallelism
 - Dynamic scheduling of user-defined tasks
 - Supports `parallel_reduce()` pattern
 - Repeated runs may not give identical results
- “Community preview” feature for reproducibility:
 - **`parallel_deterministic_reduce()`**
 - In Intel® Composer XE 2013
 - Repeated runs give identical results provided the user-supplied body yields consistent results
 - Independent of the number of threads
 - Simple partitioner always breaks up work in the same way
 - But results may differ from a serial reduction
 - May be some impact on performance

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Floating-Point Behavior on the Intel® Xeon Phi™ Coprocessor

- Floating-point exception flags are set by KCi vector instructions
 - the flags can be read
 - unmasking and trapping is not supported.
 - attempts to unmask will result in seg fault
 - -fpe0 (Fortran) and -fp-trap (C) are disabled
 - -fp-model except or strict will yield (slow!) x87 code that supports unmasking and trapping of floating-point exceptions
- Denormals are supported by KCi (but slow, like host)
 - Needs -no-ftz or -fp-model precise (like host)
- 512 bit vector transcendental math functions available (SVML)
 - Division and square root implementations still settling down
 - Both SVML and fast inlined divide and sqrt sequences available
 - Many options to select different implementations
 - See [Differences in floating-point arithmetic between Intel\(R\) Xeon processors and the Intel Xeon Phi\(TM\) coprocessor](#) for details and status

Comparing Floating-Point Results between Intel® Xeon processors and the Intel® Xeon Phi™ Coprocessor

- Different architectures – expect some differences
 - Different optimizations
 - Use of fused multiply-add (FMA)
 - Different implementations of math functions
- To minimize differences (e.g. for debugging)
 - Build with `-fp-model precise` (both architectures)
 - Build with `-no-fma` (Intel® MIC architecture)
 - Select high accuracy math functions
 - (e.g. `-fimf-precision=high`; default with `-fp-model precise`)
 - Choose reproducible parallel reductions (slides 15 & 28)
 - Or run sequentially, if you have the patience...
 - Remember, the true uncertainty of your result is probably much greater!

Further Information

- Microsoft Visual C++* Floating-Point Optimization
[http://msdn2.microsoft.com/en-us/library/aa289157\(vs.71\).aspx](http://msdn2.microsoft.com/en-us/library/aa289157(vs.71).aspx)
- The Intel® C++ and Fortran Compiler Documentation,
"Floating Point Operations"
- "Consistency of Floating-Point Results using the Intel® Compiler" <http://software.intel.com/en-us/articles/consistency-of-floating-point-results-using-the-intel-compiler/>
- "Differences in Floating-Point Arithmetic between Intel® Xeon® Processors and the Intel® Xeon Phi™ Coprocessor" <http://software.intel.com/sites/default/files/article/326703/floating-point-differences-sept11.pdf>
- Goldberg, David: "What Every Computer Scientist Should Know About Floating-Point Arithmetic" Computing Surveys, March 1991, pg. 203

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Quick Overview of Primary Switches

Primary Switches	Description
/fp:keyword	fast [= 1 2], <i>precise, source, double, extended, except, strict</i>
-fp-model keyword	<i>Controls floating point semantics</i>
/Qftz[-] -[no-]ftz	<i>Flushes denormal results to Zero</i>
<i>Some Other switches</i>	
/Qfp-speculation keyword -fp-speculation keyword	fast , <i>safe, strict, off</i> <i>floating point speculation control</i>
/Qprec-div[-] -[no-]prec-div	<i>Improves precision of floating point divides</i>
/Qprec-sqrt[-] -[no-]prec-sqrt	<i>Improves precision of square root calculations</i>
/Qfma[-] -[no-]fma	<i>Enable[Disable] use of fma instructions</i>
/Qfp-trap:... -fp-trap=common	<i>Unmask floating point exceptions (C/C++ only)</i>
/fpe:0 -fpe0	<i>Unmask floating point exceptions (Fortran only)</i>
/Qfp-port -fp-port	<i>Round floating point results to user precision</i>
/Qprec -mp1	<i>More consistent comparisons & transcendentals</i>
/Op[-] -mp [-nofltconsistency]	<i>Deprecated; use /fp:source etc instead</i>

Floating-point representations

Parameter	Single	Double	Quad or Extended Precision (IEEE_X)*
Format width in bits	32	64	128
Sign width in bits	1	1	1
mantissa	23 (24 implied)	52 (53 implied)	112 (113 implied)
Exponent width in bits	8	11	15
Max binary exponent	+127	+1023	+16383
Min binary exponent	- 126	- 1022	-16382
Exponent bias	+127	+1023	+16383
Max value	$\sim 3.4 \times 10^{38}$	$\sim 1.8 \times 10^{-308}$	$\sim 1.2 \times 10^{-4932}$
Value (Min normalized)	$\sim 1.2 \times 10^{-38}$	$\sim 2.2 \times 10^{-308}$	$\sim 3.4 \times 10^{-4932}$
Value (Min denormalized)	$\sim 1.4 \times 10^{-45}$	$\sim 4.9 \times 10^{-324}$	$\sim 6.5 \times 10^{-4966}$

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Special FP number representations

- Single precision representations

	1 Sign bit	8 Exponent bits	(1)+23 Significand bits
zero	0 or 1	0	0
denormalized	0 or 1	0	(0.)xxxxx...
normalized	0 or 1	1-254	(1.)xxxxx...
infinity	0 or 1	255	0
Signalling NaN (SNaN)	No meaning	255	(1.)0xxxx...
Quiet Nan (QNaN)	No Meaning	255	(1.)1xxxx...

Flush-To-Zero and Denormal FP Values

- A **normalized** FP number has leading binary bit and an exponent in the range accommodated by number of bits in the exponent.

- example:

$$0.171865_{10} = 1/8 + 1/32 + 1/64$$
$$= 0.001011_2$$

$$\text{normalized} = 1.011_2 \times 2^{-3}$$

- Exponent is stored in 8 bits single or 11 bits double: mantissa in 23 bits single, 52 bits double
- exponent biased by 127 (single precision)
- leading sign bit – normalized “1.” bit implied, not physically stored (1.011 stored as 011)

0 01111100 01100000000000000000000000000000

Flush-To-Zero and Denormal FP Values

- What happens if the number is close to zero BUT exponent X in the 2^{-x} won't fit in 8 or 11 bits?
- 2^{-128} for example in single precision
- Cannot represent in a NORMALIZED fashion:
- $1/2^{127} = 0.00...001_2$ (126 zeros after the binary point and a binary 1)
- $= 1.0_2 \times 2^{-128}$
- But -128 won't fit in a 127 biased 8-bit exponent value!
- Solution: DENORMAL representation
- Exponent is -126 (all zeros), NO implied leading 1.
- 0 00000000 1000000000000000000000000000

Flush-To-Zero and Denormal FP Values

- “Underflow” is when a very small number is created that cannot be represented. “gradual underflow” is when values are created that can be represented as denormal
- Denormals do not include as many significant digits
- Gradual loss of precision as denormal values get closer to zero
- *OK, fine, I like these denormal numbers, they carry some precision – why are denormals an issue?*
 - **UNFORTUNATELY denormals can cause 100x loss of performance**
- Solution: set any denormal to zero: FLUSH TO ZERO
 - Keeps performance up, tradeoff is some loss of precision and dynamic range

-prec-div and -prec-sqrt Options

- Both override the -fp-model settings
- Default is -no-prec-sqrt, and somewhere between -prec-div and -no-prec-div

[-no]-prec-div / Qprec-div[-]

- Enables[disables] various divide optimizations
 - $x / y \Leftrightarrow x * (1.0 / y)$
 - Approximate divide and reciprocal

[-no]-prec-sqrt / Qprec-sqrt[-]

- Enables[disables] approximate sqrt and reciprocal sqrt

-[no-]fast-transcendentals

The compiler frequently optimizes calls of math library functions (like exp, sinf) in loops

- Uses SVML (short vector math library) to vectorize loops
- Uses the XMM direct call routines,
e.g. exp → `___libm_sse2_exp` (IA-32 only)
 - May sometimes use fast in-lined implementations

This switch `“-[no]fast-transcendental` can be used to overwrite default behavior

- Behavior related to settings of fp-model and other switches – see reference manual !!

gcc options

- -ffast-math implies
 - -fno-math-errno
 - -funsafe-math-optimizations
 - -ffinite-math-only
 - -fno-rounding-math
 - -fno-signaling-nans
 - -fcx-limited-range
 - & sets `__FAST_MATH__`
- -funsafe-math-optimizations implies
 - -fno-signed-zeros
 - -fassociative-math
 - -fno-trapping-math
 - -freciprocal-math

Math Functions on the Intel® Xeon Phi™ Coprocessor

- Faster, more approximate versions of math functions can still be obtained with `-fp-model precise` by adding
 - `-fast-transcendentals` `-no-prec-div` `-no-prec-sqrt`
 - See [Differences in floating-point arithmetic between Intel\(R\) Xeon processors and the Intel Xeon Phi\(TM\) coprocessor](#) for details and status
- Switches for finer control of math function accuracy:
 - `-fimf-precision=<high|medium|low> [:func1,func2,...]`
 - `-fimf-max-error`
 - `-fimf-accuracy-bits`
 - `-fimf-absolute-error`
 - `-fimf-domain-exclusion`

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- Math functions have special branches and code to handle “exceptional” arguments
 - Faster versions possible if this can be skipped
- `-fimf-domain-exclusion= <value>;` the bits of `<value>` indicate domains for which the compiler need not generate special code
 - 1 extreme values (close to singularities or infinities; denormals)
 - 2 NaNs
 - 4 infinities
 - 8 denormals
 - 16 zeros
 - E.g. `-fimf-domain-exclusion=31` excludes all of these for all functions
- Can be restricted to specific functions, e.g.
 - `-fimf-domain-exclusion=15:/sqrt,sqrtf` gives fast, inlined versions of single & double precision square root
- `-fp-model-fast=2` implies `-fimf-domain-exclusion=15`